

COLLEGE ALGEBRA TRIGONOMETRIC GRAPHS

EXPLORING COLLEGE ALGEBRA TRIGONOMETRIC GRAPHS: A COMPREHENSIVE GUIDE

COLLEGE ALGEBRA TRIGONOMETRIC GRAPHS FORM A FUNDAMENTAL CORNERSTONE FOR UNDERSTANDING PERIODIC PHENOMENA ACROSS VARIOUS SCIENTIFIC AND ENGINEERING DISCIPLINES. MASTERING THESE VISUAL REPRESENTATIONS UNLOCKS A DEEPER COMPREHENSION OF CONCEPTS RANGING FROM WAVE MECHANICS AND ELECTRICAL CIRCUITS TO SOUND AND LIGHT PROPAGATION. IN COLLEGE ALGEBRA, WE MOVE BEYOND BASIC PLOTTING TO ANALYZE KEY CHARACTERISTICS THAT DEFINE THESE CYCLICAL FUNCTIONS: AMPLITUDE, PERIOD, PHASE SHIFT, AND VERTICAL SHIFT. THIS ARTICLE WILL GUIDE YOU THROUGH THE ESSENTIAL ELEMENTS OF GRAPHING SINE, COSINE, TANGENT, COSECANT, SECANT, AND COTANGENT FUNCTIONS, EQUIPPING YOU WITH THE KNOWLEDGE TO INTERPRET AND MANIPULATE THEIR VISUAL BEHAVIORS. WE'LL DELVE INTO HOW TRANSFORMATIONS AFFECT THESE GRAPHS AND EXPLORE PRACTICAL APPLICATIONS WHERE UNDERSTANDING TRIGONOMETRIC GRAPH BEHAVIOR IS CRUCIAL. PREPARE TO VISUALIZE THE FASCINATING WORLD OF PERIODIC FUNCTIONS!

TABLE OF CONTENTS

UNDERSTANDING THE BASIC TRIGONOMETRIC FUNCTIONS

THE SINE AND COSINE GRAPHS: THE FOUNDATION OF PERIODICITY

THE TANGENT GRAPH: A DIFFERENT KIND OF OSCILLATION

THE RECIPROCAL TRIGONOMETRIC GRAPHS: COSECANT, SECANT, AND COTANGENT

TRANSFORMATIONS OF TRIGONOMETRIC GRAPHS

AMPLITUDE: THE VERTICAL STRETCH

PERIOD: THE HORIZONTAL STRETCH

PHASE SHIFT: THE HORIZONTAL TRANSLATION

VERTICAL SHIFT: THE UPWARD OR DOWNWARD MOVE

GRAPHING STRATEGIES AND COMMON PITFALLS

APPLICATIONS OF TRIGONOMETRIC GRAPHS IN REAL-WORLD SCENARIOS

UNDERSTANDING THE BASIC TRIGONOMETRIC FUNCTIONS

BEFORE WE DIVE HEADFIRST INTO THE VISUAL WORLD OF TRIGONOMETRIC GRAPHS, IT'S ESSENTIAL TO HAVE A FIRM GRASP ON THE UNDERLYING TRIGONOMETRIC FUNCTIONS THEMSELVES: SINE, COSINE, TANGENT, AND THEIR RECIPROCAL. THESE FUNCTIONS RELATE ANGLES TO RATIOS OF SIDES IN RIGHT TRIANGLES, AND MORE GENERALLY, TO THE COORDINATES OF POINTS ON THE UNIT CIRCLE. THEIR INHERENT PERIODIC NATURE IS WHAT MAKES THEIR GRAPHS SO DISTINCTIVE AND USEFUL. THINK OF THEM AS THE FUNDAMENTAL BUILDING BLOCKS OF ANY CYCLICAL PATTERN YOU MIGHT ENCOUNTER, WHETHER IT'S THE SWING OF A PENDULUM OR THE EBB AND FLOW OF TIDES.

THE UNIT CIRCLE IS AN INVALUABLE TOOL FOR VISUALIZING THESE RELATIONSHIPS. AS AN ANGLE INCREASES, THE X AND Y COORDINATES OF THE POINT WHERE THE TERMINAL SIDE OF THE ANGLE INTERSECTS THE UNIT CIRCLE CORRESPOND DIRECTLY TO THE COSINE AND SINE OF THAT ANGLE, RESPECTIVELY. THIS CONNECTION IS CRUCIAL BECAUSE IT EXPLAINS WHY THESE FUNCTIONS REPEAT THEIR VALUES OVER REGULAR INTERVALS. THE TANGENT, BEING THE RATIO OF SINE TO COSINE, ALSO EXHIBITS ITS OWN UNIQUE GRAPHICAL PROPERTIES STEMMING FROM THESE FUNDAMENTAL RELATIONSHIPS. UNDERSTANDING THESE DEFINITIONS IS THE FIRST STEP TO DECIPHERING THEIR VISUAL BEHAVIOR ON A COORDINATE PLANE.

THE SINE AND COSINE GRAPHS: THE FOUNDATION OF PERIODICITY

THE SINE AND COSINE FUNCTIONS ARE ARGUABLY THE MOST FUNDAMENTAL TRIGONOMETRIC GRAPHS ENCOUNTERED IN COLLEGE ALGEBRA. THEIR SMOOTH, WAVE-LIKE PATTERNS ARE INSTANTLY RECOGNIZABLE AND FORM THE BASIS FOR UNDERSTANDING MORE COMPLEX PERIODIC FUNCTIONS. BOTH SINE AND COSINE HAVE A NATURAL PERIOD OF 2π , MEANING THEIR GRAPHS REPEAT EVERY 2π UNITS ALONG THE X-AXIS. THIS INTRINSIC REPETITION IS WHAT MAKES THEM SO POWERFUL FOR MODELING CYCLES.

THE SINE GRAPH: THE OSCILLATING WAVE

THE GRAPH OF $y = \sin(x)$ STARTS AT THE ORIGIN $(0,0)$, RISES TO A MAXIMUM VALUE OF 1 AT $x = \pi/2$, CROSSES THE X-AXIS AT $x = \pi$, REACHES A MINIMUM VALUE OF -1 AT $x = 3\pi/2$, AND RETURNS TO THE X-AXIS AT $x = 2\pi$, COMPLETING ONE FULL CYCLE. THE AMPLITUDE, WHICH IS THE MAXIMUM DISPLACEMENT FROM THE MIDLINE (THE X-AXIS IN THIS CASE), IS 1. THE PERIOD IS 2π . VISUALIZING THIS SMOOTH ASCENT AND DESCENT HELPS US UNDERSTAND HOW VALUES CHANGE INCREMENTALLY AS THE ANGLE GROWS.

THE COSINE GRAPH: THE SHIFTED SINE WAVE

THE GRAPH OF $y = \cos(x)$ IS VERY SIMILAR TO THE SINE GRAPH BUT IS SHIFTED TO THE LEFT BY $\pi/2$ RADIANS. IT BEGINS AT ITS MAXIMUM VALUE OF 1 WHEN $x = 0$, CROSSES THE X-AXIS AT $x = \pi/2$, REACHES ITS MINIMUM VALUE OF -1 AT $x = \pi$, CROSSES THE X-AXIS AGAIN AT $x = 3\pi/2$, AND RETURNS TO ITS MAXIMUM AT $x = 2\pi$. LIKE SINE, THE COSINE FUNCTION ALSO HAS AN AMPLITUDE OF 1 AND A PERIOD OF 2π . IT'S ESSENTIALLY THE SAME WAVE SHAPE, JUST STARTING AT A DIFFERENT POINT IN ITS CYCLE.

THE TANGENT GRAPH: A DIFFERENT KIND OF OSCILLATION

THE TANGENT FUNCTION, $y = \tan(x)$, PRESENTS A MORE COMPLEX GRAPHICAL BEHAVIOR THAN SINE AND COSINE DUE TO ITS DEFINITION AS THE RATIO OF SINE TO COSINE. THIS RATIO MEANS THAT TANGENT HAS POINTS WHERE IT IS UNDEFINED, SPECIFICALLY WHEN THE COSINE OF THE ANGLE IS ZERO (AT $x = \pi/2, 3\pi/2$, AND SO ON). THESE POINTS OF UNDEFINED VALUES LEAD TO VERTICAL ASYMPTOTES IN THE GRAPH.

UNDERSTANDING VERTICAL ASYMPTOTES

VERTICAL ASYMPTOTES ARE VERTICAL LINES THAT THE GRAPH APPROACHES BUT NEVER TOUCHES. FOR THE TANGENT GRAPH, THESE OCCUR AT EVERY ODD MULTIPLE OF $\pi/2$ (... , $-\pi/2, \pi/2, 3\pi/2, \dots$). BETWEEN THESE ASYMPTOTES, THE TANGENT FUNCTION RISES FROM NEGATIVE INFINITY, PASSES THROUGH THE X-AXIS AT MULTIPLES OF π (WHERE THE SINE IS ZERO), AND APPROACHES POSITIVE INFINITY. THE PERIOD OF THE TANGENT FUNCTION IS π , WHICH IS HALF THE PERIOD OF SINE AND COSINE. THIS MEANS ITS REPEATING PATTERN OCCURS OVER A SHORTER INTERVAL.

THE RECIPROCAL TRIGONOMETRIC GRAPHS: COSECANT, SECANT, AND COTANGENT

THE REMAINING TRIGONOMETRIC FUNCTIONS ARE THE RECIPROCAL OF THE PRIMARY THREE: COSECANT (CSC), SECANT (SEC), AND COTANGENT (COT). THEIR GRAPHS ARE DERIVED DIRECTLY FROM THE GRAPHS OF SINE, COSINE, AND TANGENT, RESPECTIVELY, BY TAKING THE RECIPROCAL OF THE Y-VALUES. THIS RECIPROCAL RELATIONSHIP LEADS TO DISTINCTIVE GRAPHICAL FEATURES.

THE COSECANT GRAPH: THE UNDULATING WAVES

THE COSECANT FUNCTION, $y = \csc(x)$, IS THE RECIPROCAL OF $y = \sin(x)$. WHERE $\sin(x)$ IS 0, $\csc(x)$ IS UNDEFINED, CREATING VERTICAL ASYMPTOTES AT $x = 0, \pi, 2\pi$, AND SO ON. BETWEEN THESE ASYMPTOTES, THE COSECANT GRAPH FORMS U-SHAPED CURVES OPENING UPWARDS WHERE THE SINE FUNCTION IS POSITIVE, AND INVERTED U-SHAPED CURVES OPENING DOWNWARDS

WHERE THE SINE FUNCTION IS NEGATIVE. THE MINIMUM VALUE OF THE UPWARD CURVES IS 1 , AND THE MAXIMUM VALUE OF THE DOWNWARD CURVES IS -1 . THE PERIOD OF $\csc(x)$ IS ALSO 2π .

THE SECANT GRAPH: THE U-SHAPED COMPANIONS

THE SECANT FUNCTION, $y = \sec(x)$, IS THE RECIPROCAL OF $y = \cos(x)$. SIMILAR TO COSECANT, SECANT HAS VERTICAL ASYMPTOTES WHERE $\cos(x)$ IS 0 , WHICH OCCURS AT $x = \pi/2, 3\pi/2$, AND SO ON. THE GRAPH OF SECANT CONSISTS OF U-SHAPED CURVES THAT OPEN UPWARDS WHEN COSINE IS POSITIVE AND DOWNWARDS WHEN COSINE IS NEGATIVE. THE MINIMUM VALUE OF THE UPWARD CURVES IS 1 , AND THE MAXIMUM VALUE OF THE DOWNWARD CURVES IS -1 . THE PERIOD OF $\sec(x)$ IS 2π .

THE COTANGENT GRAPH: THE INVERSE TANGENT JOURNEY

THE COTANGENT FUNCTION, $y = \cot(x)$, IS THE RECIPROCAL OF $y = \tan(x)$. COTANGENT HAS VERTICAL ASYMPTOTES WHERE $\tan(x)$ IS UNDEFINED, WHICH ARE AT $x = 0, \pi, 2\pi$, AND SO ON. THE GRAPH OF COTANGENT DECREASES FROM POSITIVE INFINITY, CROSSES THE X-AXIS AT ODD MULTIPLES OF $\pi/2$ (WHERE TANGENT IS ZERO), AND APPROACHES NEGATIVE INFINITY. THE PERIOD OF $\cot(x)$ IS π , JUST LIKE TANGENT. IT RESEMBLES THE TANGENT GRAPH BUT IS REFLECTED ACROSS THE X-AXIS AND SHIFTED.

TRANSFORMATIONS OF TRIGONOMETRIC GRAPHS

ONE OF THE MOST POWERFUL ASPECTS OF STUDYING TRIGONOMETRIC GRAPHS IN COLLEGE ALGEBRA IS UNDERSTANDING HOW TO MANIPULATE THEM THROUGH TRANSFORMATIONS. THESE TRANSFORMATIONS ALLOW US TO MODEL A VAST ARRAY OF REAL-WORLD PHENOMENA BY STRETCHING, COMPRESSING, SHIFTING, AND REFLECTING THE BASIC SINE AND COSINE CURVES. RECOGNIZING THESE CHANGES IS KEY TO INTERPRETING THE UNDERLYING DATA.

AMPLITUDE: THE VERTICAL STRETCH

THE AMPLITUDE OF A TRIGONOMETRIC FUNCTION DETERMINES THE MAXIMUM DISPLACEMENT OR "HEIGHT" OF THE WAVE FROM ITS MIDLINE. FOR A FUNCTION OF THE FORM $y = A \sin(Bx + C) + D$ OR $y = A \cos(Bx + C) + D$, THE AMPLITUDE IS GIVEN BY $|A|$. A LARGER ABSOLUTE VALUE OF A RESULTS IN A TALLER WAVE, WHILE AN A BETWEEN -1 AND 1 RESULTS IN A SHORTER WAVE. IF A IS NEGATIVE, THE GRAPH IS REFLECTED ACROSS THE X-AXIS.

PERIOD: THE HORIZONTAL STRETCH

THE PERIOD OF A TRIGONOMETRIC FUNCTION IS THE LENGTH OF ONE COMPLETE CYCLE. FOR FUNCTIONS OF THE FORM $y = A \sin(Bx + C) + D$ OR $y = A \cos(Bx + C) + D$, THE PERIOD IS CALCULATED AS $2\pi/|B|$. IF $|B| > 1$, THE PERIOD IS SHORTER THAN 2π , MEANING THE GRAPH COMPRESSES HORIZONTALLY. IF $0 < |B| < 1$, THE PERIOD IS LONGER THAN 2π , AND THE GRAPH STRETCHES HORIZONTALLY. THE TANGENT AND COTANGENT FUNCTIONS HAVE A PERIOD OF $\pi/|B|$.

PHASE SHIFT: THE HORIZONTAL TRANSLATION

A PHASE SHIFT REFERS TO THE HORIZONTAL MOVEMENT OF A TRIGONOMETRIC GRAPH. IN THE GENERAL FORMS $y = A \sin(Bx + C) + D$ AND $y = A \cos(Bx + C) + D$, THE PHASE SHIFT IS DETERMINED BY $-C/B$. A POSITIVE PHASE SHIFT MOVES THE GRAPH TO THE RIGHT, AND A NEGATIVE PHASE SHIFT MOVES IT TO THE LEFT. THIS IS LIKE SLIDING THE ENTIRE WAVE ALONG THE X-AXIS

WITHOUT CHANGING ITS SHAPE OR HEIGHT.

VERTICAL SHIFT: THE UPWARD OR DOWNWARD MOVE

THE VERTICAL SHIFT, REPRESENTED BY D IN THE GENERAL FORMS $y = A \sin(Bx + C) + D$ AND $y = A \cos(Bx + C) + D$, MOVES THE ENTIRE GRAPH UP OR DOWN. IF D IS POSITIVE, THE GRAPH SHIFTS UPWARDS; IF D IS NEGATIVE, IT SHIFTS DOWNWARDS. THIS ESSENTIALLY CHANGES THE MIDLINE OF THE GRAPH FROM THE x -AXIS ($y=0$) TO $y=D$.

GRAPHING STRATEGIES AND COMMON PITFALLS

EFFECTIVELY GRAPHING TRIGONOMETRIC FUNCTIONS REQUIRES A SYSTEMATIC APPROACH. BEGIN BY IDENTIFYING THE VALUES OF A , B , C , AND D . THESE PARAMETERS WILL TELL YOU THE AMPLITUDE, PERIOD, PHASE SHIFT, AND VERTICAL SHIFT. NEXT, DETERMINE THE KEY POINTS FOR ONE CYCLE. FOR SINE AND COSINE, THESE ARE TYPICALLY THE START OF THE CYCLE, WHERE THE FUNCTION CROSSES THE MIDLINE GOING UP, THE MAXIMUM POINT, WHERE IT CROSSES THE MIDLINE GOING DOWN, AND THE MINIMUM POINT, AND THE END OF THE CYCLE. FOR TANGENT AND COTANGENT, FOCUS ON THE ASYMPTOTES AND THE POINTS WHERE THE GRAPH CROSSES THE x -AXIS.

A COMMON PITFALL IS MISCALCULATING THE PERIOD OR PHASE SHIFT, ESPECIALLY WHEN B IS NOT A SIMPLE INTEGER. ALWAYS REMEMBER TO USE THE FORMULAS $2\pi/|B|$ (OR $\pi/|B|$ FOR TANGENT/COTANGENT) AND $-C/B$. ANOTHER ERROR IS FORGETTING TO PLOT THE VERTICAL ASYMPTOTES FOR TANGENT, COTANGENT, SECANT, AND COSECANT FUNCTIONS, WHICH ARE CRITICAL TO UNDERSTANDING THEIR BEHAVIOR. CAREFULLY IDENTIFYING THE STARTING AND ENDING x -VALUES OF ONE CYCLE IS CRUCIAL FOR ACCURATE PLOTTING. FINALLY, DOUBLE-CHECK YOUR AMPLITUDE AND VERTICAL SHIFT TO ENSURE THE WAVE IS POSITIONED AND SCALED CORRECTLY ON THE y -AXIS.

APPLICATIONS OF TRIGONOMETRIC GRAPHS IN REAL-WORLD SCENARIOS

THE ABILITY TO VISUALIZE AND UNDERSTAND TRIGONOMETRIC GRAPHS IS FAR FROM JUST AN ACADEMIC EXERCISE; IT HAS PROFOUND IMPLICATIONS FOR MODELING AND ANALYZING COUNTLESS REAL-WORLD PHENOMENA. CONSIDER THE STUDY OF SOUND WAVES. THE PITCH OF A SOUND IS RELATED TO ITS FREQUENCY, WHICH DIRECTLY IMPACTS THE PERIOD OF ITS TRIGONOMETRIC GRAPH, WHILE THE LOUDNESS CORRESPONDS TO THE AMPLITUDE. IN ELECTRICAL ENGINEERING, ALTERNATING CURRENT (AC) IS OFTEN REPRESENTED BY SINE WAVES, WHERE THE VOLTAGE AND CURRENT OSCILLATE PERIODICALLY. UNDERSTANDING THE GRAPHS HELPS IN DESIGNING CIRCUITS AND PREDICTING THEIR BEHAVIOR.

SIMILARLY, IN PHYSICS, THE MOTION OF PENDULUMS, THE OSCILLATION OF SPRINGS, AND THE PROPAGATION OF LIGHT AND ELECTROMAGNETIC WAVES ARE ALL BEAUTIFULLY DESCRIBED BY TRIGONOMETRIC FUNCTIONS AND THEIR GRAPHS. EVEN IN FIELDS LIKE BIOLOGY, THE CYCLICAL PATTERNS OF PREDATOR-PREY POPULATIONS OR SEASONAL CHANGES CAN SOMETIMES BE APPROXIMATED USING THESE PERIODIC FUNCTIONS. BEING ADEPT AT INTERPRETING COLLEGE ALGEBRA TRIGONOMETRIC GRAPHS OPENS DOORS TO A DEEPER UNDERSTANDING OF THE CYCLICAL AND WAVE-LIKE NATURE OF THE UNIVERSE AROUND US.

FAQ

Q: WHAT IS THE PRIMARY DIFFERENCE BETWEEN THE GRAPHS OF SINE AND COSINE?

A: THE PRIMARY DIFFERENCE BETWEEN THE GRAPHS OF SINE AND COSINE IS THEIR PHASE. THE COSINE GRAPH IS ESSENTIALLY A SINE GRAPH SHIFTED TO THE LEFT BY $\pi/2$ RADIANS, MEANING IT STARTS AT ITS MAXIMUM VALUE AT $x=0$, WHEREAS THE SINE GRAPH STARTS AT 0.

Q: HOW DO VERTICAL ASYMPTOTES AFFECT THE GRAPH OF A TRIGONOMETRIC FUNCTION?

A: VERTICAL ASYMPTOTES INDICATE POINTS WHERE THE TRIGONOMETRIC FUNCTION IS UNDEFINED. FOR GRAPHS LIKE TANGENT, COTANGENT, SECANT, AND COSECANT, THESE ASYMPTOTES CREATE BREAKS IN THE GRAPH, AND THE FUNCTION'S VALUES APPROACH INFINITY OR NEGATIVE INFINITY AS THEY GET CLOSER TO THESE LINES.

Q: WHAT DOES THE 'PERIOD' OF A TRIGONOMETRIC GRAPH REPRESENT?

A: THE PERIOD OF A TRIGONOMETRIC GRAPH REPRESENTS THE LENGTH OF ONE COMPLETE CYCLE OF THE FUNCTION. IT TELLS YOU HOW OFTEN THE GRAPH REPEATS ITS PATTERN ALONG THE X-AXIS.

Q: HOW CAN I QUICKLY DETERMINE THE AMPLITUDE OF A TRIGONOMETRIC FUNCTION?

A: THE AMPLITUDE IS THE ABSOLUTE VALUE OF THE COEFFICIENT MULTIPLYING THE SINE OR COSINE FUNCTION. FOR EXAMPLE, IN THE FUNCTION $y = 3\sin(x)$, THE AMPLITUDE IS 3, MEANING THE GRAPH OSCILLATES 3 UNITS ABOVE AND 3 UNITS BELOW ITS MIDLINE.

Q: WHAT IS A PHASE SHIFT AND HOW DOES IT CHANGE A TRIGONOMETRIC GRAPH?

A: A PHASE SHIFT IS A HORIZONTAL TRANSLATION OF THE GRAPH. IT MOVES THE ENTIRE GRAPH TO THE LEFT OR RIGHT WITHOUT ALTERING ITS SHAPE, AMPLITUDE, OR PERIOD. IT'S OFTEN REPRESENTED BY THE TERM ADDED OR SUBTRACTED INSIDE THE TRIGONOMETRIC FUNCTION.

Q: WHY IS IT IMPORTANT TO UNDERSTAND TRIGONOMETRIC GRAPHS IN COLLEGE ALGEBRA?

A: UNDERSTANDING TRIGONOMETRIC GRAPHS IS CRUCIAL BECAUSE THEY VISUALLY REPRESENT PERIODIC PHENOMENA FOUND IN MANY REAL-WORLD APPLICATIONS, SUCH AS WAVE MOTION, OSCILLATIONS, AND CYCLES. THIS GRAPHICAL UNDERSTANDING AIDS IN PROBLEM-SOLVING AND CONCEPTUALIZATION IN PHYSICS, ENGINEERING, AND MATHEMATICS.

Q: HOW DOES CHANGING THE 'B' VALUE IN $y = A\sin(Bx)$ AFFECT THE GRAPH?

A: CHANGING THE 'B' VALUE AFFECTS THE PERIOD OF THE GRAPH. THE NEW PERIOD IS CALCULATED AS $2\pi/|B|$. IF $|B| > 1$, THE PERIOD SHORTENS, AND THE GRAPH APPEARS COMPRESSED HORIZONTALLY. IF $0 < |B| < 1$, THE PERIOD LENGTHENS, AND THE GRAPH STRETCHES HORIZONTALLY.

Q: CAN TANGENT AND COTANGENT FUNCTIONS HAVE AMPLITUDE?

A: BY DEFINITION, TANGENT AND COTANGENT FUNCTIONS DO NOT HAVE A MAXIMUM OR MINIMUM VALUE, AS THEY EXTEND TO POSITIVE AND NEGATIVE INFINITY AND HAVE VERTICAL ASYMPTOTES. THEREFORE, THEY DO NOT HAVE AN AMPLITUDE IN THE SAME WAY THAT SINE AND COSINE FUNCTIONS DO.

Q: WHAT IS THE ROLE OF THE VERTICAL SHIFT IN A TRIGONOMETRIC GRAPH?

A: THE VERTICAL SHIFT MOVES THE ENTIRE GRAPH UP OR DOWN. IT CHANGES THE MIDLINE OF THE GRAPH FROM THE X-AXIS ($y=0$) TO A NEW HORIZONTAL LINE, $y = D$, WHERE D IS THE VERTICAL SHIFT.

College Algebra Trigonometric Graphs

College Algebra Trigonometric Graphs

Related Articles

- [college algebra trig for beginners](#)
- [college algebra tests](#)
- [college algebra trig review college](#)

[Back to Home](#)