

COLLEGE ALGEBRA FINAL EXAM REVIEW INEQUALITIES

COLLEGE ALGEBRA FINAL EXAM REVIEW INEQUALITIES CAN FEEL DAUNTING, BUT WITH A STRUCTURED APPROACH, MASTERING THIS CRUCIAL TOPIC IS ENTIRELY ACHIEVABLE. THIS COMPREHENSIVE REVIEW GUIDE IS DESIGNED TO EQUIP YOU WITH THE KNOWLEDGE AND STRATEGIES NECESSARY TO EXCEL ON YOUR COLLEGE ALGEBRA FINAL EXAM, SPECIFICALLY FOCUSING ON THE DIVERSE LANDSCAPE OF INEQUALITIES. WE WILL DELVE INTO THE FUNDAMENTAL PRINCIPLES OF LINEAR INEQUALITIES, EXPLORE THE INTRICACIES OF QUADRATIC AND RATIONAL INEQUALITIES, AND EXAMINE COMPOUND AND ABSOLUTE VALUE INEQUALITIES. FURTHERMORE, WE WILL DISCUSS IMPORTANT CONCEPTS LIKE INTERVAL NOTATION AND GRAPHICAL REPRESENTATIONS, ALL VITAL FOR A THOROUGH UNDERSTANDING AND SUCCESSFUL APPLICATION. BY THE END OF THIS REVIEW, YOU WILL POSSESS A ROBUST UNDERSTANDING OF INEQUALITY SOLVING TECHNIQUES, PREPARING YOU TO CONFIDENTLY TACKLE ANY INEQUALITY-RELATED PROBLEMS THAT APPEAR ON YOUR EXAM.

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UNDERSTANDING LINEAR INEQUALITIES

LINEAR INEQUALITIES ARE THE BEDROCK OF INEQUALITY CONCEPTS IN COLLEGE ALGEBRA. THEY INVOLVE EXPRESSIONS WITH A SINGLE VARIABLE RAISED TO THE POWER OF ONE, CONNECTED BY INEQUALITY SYMBOLS SUCH AS LESS THAN ($<$), GREATER THAN ($>$), LESS THAN OR EQUAL TO ($\leq$), OR GREATER THAN OR EQUAL TO ($\geq$). THE FUNDAMENTAL APPROACH TO SOLVING LINEAR INEQUALITIES MIRRORS THAT OF SOLVING LINEAR EQUATIONS, WITH ONE CRITICAL DISTINCTION: WHEN MULTIPLYING OR DIVIDING BOTH SIDES OF AN INEQUALITY BY A NEGATIVE NUMBER, THE DIRECTION OF THE INEQUALITY SYMBOL MUST BE REVERSED.

CONSIDER A BASIC EXAMPLE: $2x + 3 < 7$. TO ISOLATE x , WE FIRST SUBTRACT 3 FROM BOTH SIDES, YIELDING $2x < 4$. NEXT, WE DIVIDE BY 2, RESULTING IN $x < 2$. THIS MEANS ALL REAL NUMBERS LESS THAN 2 SATISFY THE ORIGINAL INEQUALITY. REPRESENTING THIS SOLUTION SET IS OFTEN DONE USING INTERVAL NOTATION, WHERE IT WOULD BE WRITTEN AS $(-\infty, 2)$. UNDERSTANDING THIS FOUNDATIONAL PRINCIPLE IS PARAMOUNT FOR PROGRESSING TO MORE COMPLEX INEQUALITY TYPES.

SOLVING ONE-VARIABLE LINEAR INEQUALITIES

THE PROCESS OF SOLVING ONE-VARIABLE LINEAR INEQUALITIES INVOLVES ISOLATING THE VARIABLE USING INVERSE OPERATIONS, SIMILAR TO SOLVING LINEAR EQUATIONS. HOWEVER, VIGILANCE IS REQUIRED WHEN DEALING WITH NEGATIVE COEFFICIENTS. FOR INSTANCE, IF YOU ENCOUNTER $-3x + 5 > 11$, YOU WOULD FIRST SUBTRACT 5 FROM BOTH SIDES TO GET $-3x > 6$. AT THIS STAGE, DIVIDING BY -3 NECESSITATES FLIPPING THE INEQUALITY SIGN, TRANSFORMING IT INTO $x < -2$. THEREFORE, THE SOLUTION SET INCLUDES ALL NUMBERS LESS THAN -2 .

WORKING WITH MULTI-STEP LINEAR INEQUALITIES

MULTI-STEP LINEAR INEQUALITIES OFTEN INVOLVE COMBINING LIKE TERMS, DISTRIBUTING, AND THEN ISOLATING THE VARIABLE. THE CORE PRINCIPLES REMAIN THE SAME. FOR EXAMPLE, TO SOLVE $3(x - 1) + 2x \leq 11$, FIRST DISTRIBUTE THE 3: $3x - 3 + 2x \leq 11$. COMBINE LIKE TERMS: $5x - 3 \leq 11$. ADD 3 TO BOTH SIDES: $5x \leq 14$. FINALLY, DIVIDE BY 5: $x \leq 14/5$. THIS SOLUTION SET ENCOMPASSES ALL REAL NUMBERS LESS THAN OR EQUAL TO $14/5$.

SOLVING QUADRATIC INEQUALITIES

QUADRATIC INEQUALITIES INVOLVE A VARIABLE RAISED TO THE POWER OF TWO, TYPICALLY IN THE FORM $ax^2 + bx + c < 0$, $ax^2 + bx + c > 0$, OR WITH EQUALITY. THE METHOD FOR SOLVING THESE DIFFERS SIGNIFICANTLY FROM LINEAR INEQUALITIES. THE FIRST STEP IS TO FIND THE ROOTS OF THE CORRESPONDING QUADRATIC EQUATION ($ax^2 + bx + c = 0$). THESE ROOTS DIVIDE THE NUMBER LINE INTO INTERVALS. WE THEN TEST A VALUE FROM EACH INTERVAL IN THE ORIGINAL INEQUALITY TO DETERMINE WHICH INTERVALS SATISFY THE CONDITION.

FOR EXAMPLE, TO SOLVE $x^2 - 5x + 6 > 0$, WE FIRST FIND THE ROOTS OF $x^2 - 5x + 6 = 0$. FACTORING GIVES US $(x - 2)(x - 3) = 0$, SO THE ROOTS ARE $x = 2$ AND $x = 3$. THESE ROOTS DIVIDE THE NUMBER LINE INTO THREE INTERVALS: $(-\infty, 2)$, $(2, 3)$, AND $(3, \infty)$. TESTING A VALUE FROM EACH INTERVAL (E.G., $x=0$, $x=2.5$, $x=4$) IN THE ORIGINAL INEQUALITY $x^2 - 5x + 6 > 0$ WILL REVEAL THE SOLUTION. FOR $x=0$, $6 > 0$ (TRUE). FOR $x=2.5$, $6.25 - 12.5 + 6 = -0.25 > 0$ (FALSE). FOR $x=4$, $16 - 20 + 6 = 2 > 0$ (TRUE). THUS, THE SOLUTION IS $(-\infty, 2) \cup (3, \infty)$.

FINDING ROOTS OF QUADRATIC EQUATIONS

THE ABILITY TO ACCURATELY FIND THE ROOTS OF A QUADRATIC EQUATION IS FUNDAMENTAL TO SOLVING QUADRATIC INEQUALITIES. THIS CAN BE ACHIEVED THROUGH VARIOUS METHODS, INCLUDING FACTORING, COMPLETING THE SQUARE, OR USING THE QUADRATIC FORMULA ($x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$). WHICHEVER METHOD IS EMPLOYED, ENSURE THE EQUATION IS SET TO ZERO BEFORE PROCEEDING TO IDENTIFY THESE CRITICAL BOUNDARY POINTS ON THE NUMBER LINE.

USING TEST VALUES FOR INTERVAL VERIFICATION

ONCE THE ROOTS OF THE QUADRATIC EQUATION HAVE BEEN DETERMINED, THEY SERVE AS THE DIVIDING POINTS FOR INTERVALS ON THE NUMBER LINE. FOR EACH OF THESE INTERVALS, IT IS CRUCIAL TO SELECT A REPRESENTATIVE TEST VALUE. SUBSTITUTING THIS TEST VALUE INTO THE ORIGINAL QUADRATIC INEQUALITY WILL DEFINITELY TELL YOU WHETHER THAT ENTIRE INTERVAL IS PART OF THE SOLUTION SET. THIS SYSTEMATIC APPROACH GUARANTEES ACCURACY IN IDENTIFYING THE CORRECT SOLUTION INTERVALS.

MASTERING RATIONAL INEQUALITIES

RATIONAL INEQUALITIES INVOLVE RATIONAL EXPRESSIONS, WHICH ARE FRACTIONS WHERE THE NUMERATOR AND/OR DENOMINATOR CONTAIN VARIABLES. SOLVING THESE REQUIRES AN UNDERSTANDING OF BOTH POLYNOMIAL INEQUALITIES AND THE RESTRICTIONS ON THE VARIABLE (VALUES THAT MAKE THE DENOMINATOR ZERO). THE CRITICAL VALUES FOR RATIONAL INEQUALITIES ARE THE ROOTS OF THE NUMERATOR (WHERE THE EXPRESSION EQUALS ZERO) AND THE ROOTS OF THE DENOMINATOR (WHERE THE EXPRESSION IS UNDEFINED).

FOR INSTANCE, TO SOLVE $(x - 1) / (x + 2) \geq 0$, THE CRITICAL VALUES ARE $x = 1$ (FROM THE NUMERATOR) AND $x = -2$ (FROM THE DENOMINATOR). THESE VALUES DIVIDE THE NUMBER LINE INTO THREE INTERVALS: $(-\infty, -2)$, $(-2, 1)$, AND $(1, \infty)$. WE MUST ALSO CONSIDER THAT x CANNOT BE -2 . TESTING VALUES IN EACH INTERVAL (E.G., $x=-3$, $x=0$, $x=2$) IN THE ORIGINAL INEQUALITY WILL REVEAL THE SOLUTION. FOR $x=-3$, $(-4)/(-1) = 4 \geq 0$ (TRUE). FOR $x=0$, $(-1)/2 = -0.5 \geq 0$ (FALSE). FOR $x=2$, $(1)/4 = 0.25 \geq 0$ (TRUE). ADDITIONALLY, SINCE THE INEQUALITY INCLUDES "OR EQUAL TO," WE CHECK IF $x=1$ SATISFIES THE INEQUALITY: $(0)/3 = 0 \geq 0$ (TRUE). THUS, THE SOLUTION IS $(-\infty, -2) \cup [1, \infty)$.

IDENTIFYING CRITICAL VALUES FROM NUMERATOR AND DENOMINATOR

THE CRITICAL VALUES IN RATIONAL INEQUALITIES ARE THE SOLUTIONS TO THE EQUATION FORMED BY SETTING THE NUMERATOR EQUAL TO ZERO AND THE SOLUTIONS TO THE EQUATION FORMED BY SETTING THE DENOMINATOR EQUAL TO ZERO. THESE VALUES ARE PIVOTAL BECAUSE THEY ARE THE ONLY POINTS WHERE THE RATIONAL EXPRESSION CAN CHANGE ITS SIGN. IT IS IMPERATIVE TO REMEMBER THAT ANY VALUE THAT MAKES THE DENOMINATOR ZERO IS NEVER PART OF THE SOLUTION SET.

HANDLING DENOMINATOR RESTRICTIONS

A FUNDAMENTAL ASPECT OF RATIONAL INEQUALITIES IS ACKNOWLEDGING THAT DIVISION BY ZERO IS UNDEFINED. THEREFORE, ANY VALUE OF THE VARIABLE THAT CAUSES THE DENOMINATOR OF THE RATIONAL EXPRESSION TO BE ZERO MUST BE EXCLUDED FROM THE SOLUTION SET. THIS EXCLUSION IS TYPICALLY REPRESENTED BY OPEN CIRCLES ON A NUMBER LINE OR BY USING PARENTHESES IN INTERVAL NOTATION AT THOSE SPECIFIC POINTS.

CONQUERING COMPOUND INEQUALITIES

COMPOUND INEQUALITIES INVOLVE TWO OR MORE INEQUALITIES JOINED BY THE CONJUNCTIONS "AND" OR "OR." WHEN INEQUALITIES ARE JOINED BY "AND," THE SOLUTION SET INCLUDES VALUES THAT SATISFY BOTH INEQUALITIES SIMULTANEOUSLY. WHEN JOINED BY "OR," THE SOLUTION SET INCLUDES VALUES THAT SATISFY AT LEAST ONE OF THE INEQUALITIES.

FOR EXAMPLE, A COMPOUND INEQUALITY WITH "AND" MIGHT BE $2x + 1 > 5$ AND $3x - 2 \leq 7$. SOLVING THE FIRST INEQUALITY GIVES $x > 2$. SOLVING THE SECOND GIVES $x \leq 3$. FOR BOTH TO BE TRUE, x MUST BE GREATER THAN 2 AND LESS THAN OR EQUAL TO 3, WHICH IS REPRESENTED AS $2 < x \leq 3$ OR IN INTERVAL NOTATION AS $(2, 3]$. CONVERSELY, AN "OR" COMPOUND INEQUALITY COULD BE $x - 4 < -1$ OR $2x + 5 \geq 11$. THE FIRST INEQUALITY YIELDS $x < 3$, AND THE SECOND YIELDS $x \geq 3$. THE SOLUTION FOR "OR" IS ALL REAL NUMBERS, $x \in (-\infty, 3) \cup [3, \infty)$.

INTERPRETING "AND" CONJUNCTIONS

WHEN INEQUALITIES ARE CONNECTED BY "AND," YOU ARE SEEKING THE INTERSECTION OF THE SOLUTION SETS OF THE INDIVIDUAL INEQUALITIES. GRAPHICALLY, THIS MEANS FINDING THE REGION WHERE THE SHADED AREAS OF BOTH INEQUALITIES OVERLAP ON THE NUMBER LINE OR COORDINATE PLANE. THE RESULTING SOLUTION SET WILL BE A SUBSET OF THE SOLUTIONS FOR EACH INDIVIDUAL INEQUALITY.

INTERPRETING "OR" CONJUNCTIONS

THE "OR" CONJUNCTION REQUIRES FINDING THE UNION OF THE SOLUTION SETS. THIS MEANS ANY VALUE SATISFYING EITHER ONE OF THE INEQUALITIES, OR BOTH, IS INCLUDED IN THE SOLUTION. GRAPHICALLY, THIS INVOLVES COMBINING ALL SHADED REGIONS FROM THE INDIVIDUAL INEQUALITIES. THE SOLUTION SET FOR AN "OR" COMPOUND INEQUALITY IS OFTEN BROADER THAN THE SOLUTIONS OF ITS CONSTITUENT INEQUALITIES.

TACKLING ABSOLUTE VALUE INEQUALITIES

ABSOLUTE VALUE INEQUALITIES DEAL WITH THE DISTANCE OF A NUMBER FROM ZERO. AN INEQUALITY OF THE FORM $|ax + b| < c$ IS EQUIVALENT TO $-c < ax + b < c$, REPRESENTING VALUES WHOSE DISTANCE FROM ZERO IS LESS THAN c . CONVERSELY, AN INEQUALITY OF THE FORM $|ax + b| > c$ IS EQUIVALENT TO $ax + b < -c$ OR $ax + b > c$, REPRESENTING VALUES WHOSE DISTANCE FROM ZERO IS GREATER THAN c .

CONSIDER THE INEQUALITY $|2x - 1| \leq 5$. THIS CAN BE REWRITTEN AS $-5 \leq 2x - 1 \leq 5$. ADDING 1 TO ALL PARTS GIVES $-4 \leq 2x \leq 6$. DIVIDING BY 2 YIELDS $-2 \leq x \leq 3$. FOR AN INEQUALITY LIKE $|x + 3| > 4$, WE SPLIT IT INTO TWO SEPARATE INEQUALITIES: $x + 3 < -4$ OR $x + 3 > 4$. SOLVING THE FIRST GIVES $x < -7$, AND SOLVING THE SECOND GIVES $x > 1$. THE SOLUTION IS THEREFORE $x < -7$ OR $x > 1$, OR IN INTERVAL NOTATION, $(-\infty, -7) \cup (1, \infty)$.

ABSOLUTE VALUE INEQUALITIES OF THE FORM $|x| < c$

WHEN THE ABSOLUTE VALUE EXPRESSION IS LESS THAN A CONSTANT (E.G., $|ax + b| < c$), THE SOLUTION REPRESENTS VALUES WITHIN A CERTAIN RANGE. THIS IS BROKEN DOWN INTO A COMPOUND INEQUALITY: $-c < ax + b < c$. THE SOLUTION SET WILL BE A SINGLE BOUNDED INTERVAL ON THE NUMBER LINE.

ABSOLUTE VALUE INEQUALITIES OF THE FORM $|X| > c$

FOR ABSOLUTE VALUE INEQUALITIES WHERE THE EXPRESSION IS GREATER THAN A CONSTANT (E.G., $|AX + B| > c$), THE SOLUTION INDICATES VALUES OUTSIDE A CERTAIN RANGE. THIS IS RESOLVED BY CREATING TWO SEPARATE INEQUALITIES CONNECTED BY "OR": $AX + B < -c$ OR $AX + B > c$. THE SOLUTION SET TYPICALLY CONSISTS OF TWO DISJOINT INTERVALS.

GRAPHICAL REPRESENTATIONS OF INEQUALITIES

VISUALIZING INEQUALITIES ON A NUMBER LINE OR A COORDINATE PLANE SIGNIFICANTLY AIDS IN UNDERSTANDING THEIR SOLUTION SETS. FOR ONE-VARIABLE INEQUALITIES, A NUMBER LINE IS USED. OPEN CIRCLES INDICATE THAT THE ENDPOINT IS NOT INCLUDED IN THE SOLUTION (FOR $<$ OR $>$), WHILE CLOSED CIRCLES INDICATE THAT THE ENDPOINT IS INCLUDED (FOR $\leq$ OR $\geq$). THE SOLUTION SET IS THEN REPRESENTED BY SHADING THE APPROPRIATE REGION ON THE LINE.

FOR TWO-VARIABLE INEQUALITIES, SUCH AS $y > 2x + 1$, A COORDINATE PLANE IS USED. FIRST, THE BOUNDARY LINE ($y = 2x + 1$) IS GRAPHED. IF THE INEQUALITY IS STRICT ($<$ OR $>$), THE LINE IS DASHED. IF IT INCLUDES EQUALITY ($\leq$ OR $\geq$), THE LINE IS SOLID. THEN, A TEST POINT (LIKE $(0,0)$) IS USED TO DETERMINE WHICH SIDE OF THE LINE TO SHADE. IF $(0,0)$ SATISFIES THE INEQUALITY, SHADE THE SIDE CONTAINING $(0,0)$; OTHERWISE, SHADE THE OPPOSITE SIDE. FOR EXAMPLE, FOR $y > 2x + 1$, TESTING $(0,0)$ YIELDS $0 > 2(0) + 1$, OR $0 > 1$, WHICH IS FALSE. THEREFORE, WE SHADE THE REGION ABOVE THE DASHED LINE $y = 2x + 1$.

NUMBER LINE VISUALIZATIONS FOR ONE-VARIABLE INEQUALITIES

THE NUMBER LINE PROVIDES A CLEAR AND CONCISE WAY TO DEPICT THE SOLUTION SETS OF INEQUALITIES INVOLVING A SINGLE VARIABLE. CRITICAL POINTS ARE MARKED, AND THE INTERVALS THAT SATISFY THE INEQUALITY ARE SHADED. THIS VISUAL REPRESENTATION REINFORCES THE ALGEBRAIC SOLUTION AND MAKES IT EASIER TO GRASP THE RANGE OF VALUES THAT ARE VALID.

COORDINATE PLANE GRAPHS FOR TWO-VARIABLE INEQUALITIES

WHEN DEALING WITH INEQUALITIES INVOLVING TWO VARIABLES, THE GRAPH ON A COORDINATE PLANE BECOMES ESSENTIAL. THE BOUNDARY LINE SEPARATES THE PLANE INTO REGIONS, AND SHADING INDICATES THE HALF-PLANE THAT CONSTITUTES THE SOLUTION SET. THE TYPE OF LINE (SOLID OR DASHED) AND THE DIRECTION OF SHADING ARE DETERMINED BY THE INEQUALITY SYMBOL.

THE IMPORTANCE OF INTERVAL NOTATION

INTERVAL NOTATION IS A STANDARDIZED AND EFFICIENT METHOD FOR EXPRESSING SOLUTION SETS, PARTICULARLY FOR INEQUALITIES. IT USES PARENTHESES TO INDICATE THAT AN ENDPOINT IS NOT INCLUDED (SIMILAR TO OPEN CIRCLES ON A NUMBER LINE) AND SQUARE BRACKETS TO INDICATE THAT AN ENDPOINT IS INCLUDED (SIMILAR TO CLOSED CIRCLES). THE SYMBOL ∞ (INFINITY) AND $-\infty$ (NEGATIVE INFINITY) ARE ALWAYS USED WITH PARENTHESES BECAUSE THEY ARE NOT ACTUAL NUMBERS AND THUS CANNOT BE INCLUDED IN A SOLUTION SET.

FOR EXAMPLE, THE SOLUTION $x < 5$ IS WRITTEN AS $(-\infty, 5)$. THE SOLUTION $x \geq 2$ IS WRITTEN AS $[2, \infty)$. WHEN A SOLUTION CONSISTS OF MULTIPLE DISJOINT INTERVALS, THE UNION SYMBOL ($\cup$) IS USED. FOR INSTANCE, THE SOLUTION $x < -2$ OR $x > 1$ WOULD BE WRITTEN AS $(-\infty, -2) \cup (1, \infty)$. MASTERING INTERVAL NOTATION IS CRUCIAL FOR PRESENTING ANSWERS CLEARLY AND ACCURATELY ON YOUR COLLEGE ALGEBRA FINAL EXAM, AS IT IS OFTEN THE REQUIRED FORMAT.

UNDERSTANDING PARENTHESES AND BRACKETS

THE DISTINCTION BETWEEN PARENTHESES AND SQUARE BRACKETS IN INTERVAL NOTATION IS CRITICAL FOR ACCURATELY REPRESENTING WHETHER AN ENDPOINT IS INCLUDED IN THE SOLUTION SET. PARENTHESES ARE USED FOR OPEN INTERVALS (ENDPOINTS EXCLUDED), WHILE BRACKETS ARE USED FOR CLOSED INTERVALS (ENDPOINTS INCLUDED). THIS DETAIL IS NON-

USING THE UNION SYMBOL

THE UNION SYMBOL ($\cup$) IS EMPLOYED WHEN THE SOLUTION TO AN INEQUALITY COMPRISES TWO OR MORE SEPARATE INTERVALS. IT SIGNIFIES THAT ANY VALUE WITHIN ANY OF THESE LISTED INTERVALS IS A VALID SOLUTION. EFFECTIVELY USING THE UNION SYMBOL ENSURES THAT THE ENTIRETY OF THE SOLUTION SET IS ACCURATELY CONVEYED IN INTERVAL NOTATION.

Q: WHAT IS THE MOST COMMON MISTAKE STUDENTS MAKE WHEN SOLVING LINEAR INEQUALITIES?

A: THE MOST COMMON MISTAKE IS FORGETTING TO REVERSE THE INEQUALITY SIGN WHEN MULTIPLYING OR DIVIDING BOTH SIDES BY A NEGATIVE NUMBER. THIS ERROR FUNDAMENTALLY ALTERS THE SOLUTION SET AND LEADS TO INCORRECT ANSWERS.

Q: HOW DO I DETERMINE THE TEST VALUES FOR QUADRATIC INEQUALITIES?

A: AFTER FINDING THE ROOTS OF THE CORRESPONDING QUADRATIC EQUATION, THESE ROOTS DIVIDE THE NUMBER LINE INTO INTERVALS. CHOOSE ANY SINGLE NUMBER WITHIN EACH OF THESE INTERVALS AS YOUR TEST VALUE. FOR EXAMPLE, IF THE ROOTS ARE 2 AND 5, THE INTERVALS ARE $(-\infty, 2)$, $(2, 5)$, AND $(5, \infty)$. YOU COULD CHOOSE -1, 3, AND 6 AS YOUR TEST VALUES, RESPECTIVELY.

Q: ARE THERE ANY SPECIAL CONSIDERATIONS FOR INEQUALITIES INVOLVING ZERO IN THE DENOMINATOR?

A: YES, ANY VALUE THAT MAKES THE DENOMINATOR OF A RATIONAL EXPRESSION EQUAL TO ZERO MUST ALWAYS BE EXCLUDED FROM THE SOLUTION SET. THIS IS BECAUSE DIVISION BY ZERO IS UNDEFINED. THESE VALUES ARE TYPICALLY REPRESENTED WITH OPEN CIRCLES ON A NUMBER LINE OR PARENTHESES IN INTERVAL NOTATION.

Q: HOW CAN I VISUALLY CHECK IF MY ABSOLUTE VALUE INEQUALITY SOLUTION IS CORRECT?

A: YOU CAN GRAPH THE RELATED ABSOLUTE VALUE FUNCTION (E.G., $y = |ax + b|$) AND THE CONSTANT VALUE (E.G., $y = c$) ON THE SAME COORDINATE PLANE. FOR $|ax + b| < c$, LOOK FOR THE X-VALUES WHERE THE GRAPH OF THE ABSOLUTE VALUE FUNCTION IS BELOW THE HORIZONTAL LINE. FOR $|ax + b| > c$, LOOK FOR THE X-VALUES WHERE THE GRAPH IS ABOVE THE HORIZONTAL LINE.

Q: WHAT DOES IT MEAN WHEN A SOLUTION TO AN INEQUALITY IS THE ENTIRE REAL NUMBER LINE?

A: IF THE SOLUTION SET TO AN INEQUALITY IS ALL REAL NUMBERS, IT MEANS THAT EVERY POSSIBLE REAL NUMBER SATISFIES THE ORIGINAL INEQUALITY. THIS OFTEN OCCURS WITH ABSOLUTE VALUE INEQUALITIES WHERE THE EXPRESSION IS LESS THAN A NON-NEGATIVE NUMBER THAT IS GREATER THAN OR EQUAL TO ZERO (E.G., $|x| \leq 0$), OR WHEN SIMPLIFYING LEADS TO A TRUE STATEMENT LIKE $5 = 5$.

Q: HOW DO I GRAPH A COMPOUND INEQUALITY ON A NUMBER LINE?

A: FOR AN "AND" COMPOUND INEQUALITY, YOU ARE LOOKING FOR THE INTERSECTION OF THE TWO SOLUTION SETS. GRAPH

EACH INEQUALITY SEPARATELY AND THEN SHADE ONLY THE REGION WHERE BOTH SHADED AREAS OVERLAP. FOR AN "OR" COMPOUND INEQUALITY, YOU TAKE THE UNION OF THE TWO SOLUTION SETS, MEANING YOU SHADE ALL REGIONS THAT ARE SHADED BY EITHER INEQUALITY.

Q: CAN INTERVAL NOTATION REPRESENT INFINITE SOLUTIONS?

A: YES, INTERVAL NOTATION CAN REPRESENT INFINITE SOLUTIONS USING THE INFINITY SYMBOL (∞) AND NEGATIVE INFINITY SYMBOL ($-\infty$). THESE SYMBOLS ARE ALWAYS PAIRED WITH PARENTHESES, AS INFINITY IS NOT A SPECIFIC NUMBER AND THEREFORE CANNOT BE INCLUDED IN THE SET. FOR EXAMPLE, ALL REAL NUMBERS GREATER THAN 5 IS WRITTEN AS $(5, \infty)$.

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